## Monoprotic Acid/Base Equilibria

## SWITCHED TO HARRIS TEXT

## THIS WEEK IS THE LAST WEEK FOR IN-PERSON LABS

## 9-2 Weak Acids and Bases

9-3 Weak Acid Equilibria
9-4 Weak Base Equilibria
9-5 Buffers (Friday)

## Acid/Base Strengths

acid strength - determined by extent of reaction of acid with water to form $\mathrm{H}_{3} \mathrm{O}^{+}(a q)$, or the extent of its ionization or dissociation, as shown by the magnitude of its equilibrium constant, $K_{a}$ - then for any hydrogen-containing compound, HA

$K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}$
EQUILIBRIUM CONSTANT
base strength - (aside from Group I and II hydroxides) determined by extent of reaction of base with water to form $\mathrm{OH}^{-}(\mathrm{aq})$, or extent of its ionization, as shown by the magnitude of its equilibrium constant, $K_{\mathrm{b}}$ - then for any base B :
$\mathrm{B}:(\mathrm{aq}) \quad+\quad \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \quad<=>\quad \mathrm{OH}^{-}(\mathrm{aq}) \quad+\quad \mathrm{BH}^{+}(\mathrm{aq})$
EQUATION FOR BASICITY FOR ANY B:


## Conjugate Acid/Base Pairs

The conjugate base of a weak acid is a weak base. The weaker the acid, the stronger the base. However, if one member of a conjugate pair is weak, so is its conjugate.

The relation between $K_{\mathrm{a}}$ for an acid and $K_{\mathrm{b}}$ for its conjugate base in aqueous solution is $K_{\mathrm{w}}=K_{\mathrm{a}} \times K_{\mathrm{b}}$.

When a strong acid (or base) is added to a weak base (or acid), they react nearly completely.


## Systematic Treatment of Equilibrium

GOAL - account for the concentration of all species present in a solution once equilibrium has been reached. The equations to do this derive from

1. charge balance - solution must be electrically neutral
2. material balance - conservation of matter; what happens to initial concentrations
3. equilibrium expressions and their equilibrium constants

## Systematic Treatment of Equilibrium - Charge Balance

salt
EX 2. Write the charge balance for a solution containing $\left(\mathrm{NH}_{4}\right)_{3} \mathrm{PO}_{4}$. Be sure to consider all possible equilibrium reactions.
$\mathrm{NH}_{4}{ }^{+}$is an acid but its equilibrium reaction produces its neutral conjugate base, $\mathrm{NH}_{3} ; \mathrm{PO}_{4}{ }^{3-}$ is a base whose equilibrium reactions produce

$$
\begin{aligned}
& \mathrm{PO}_{4}^{3-}+\mathrm{H}_{2} \mathrm{O}<=>\mathrm{OH}^{-}+\mathrm{HPO}_{4}^{2-} \\
& \mathrm{HPO}_{4}^{2-}+\mathrm{H}_{2} \mathrm{O}<=>\mathrm{OH}^{-}+\mathrm{H}_{2} \mathrm{PO}_{4}^{-} \\
& \mathrm{H}_{2} \mathrm{PO}_{4}^{-}+\mathrm{H}_{2} \mathrm{O}
\end{aligned}=>\mathrm{OH}^{-}+\mathrm{H}_{3} \mathrm{PO}_{4}-2
$$

in aqueous solution autoionization of water must always be considered:
$\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}<=>\mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{OH}^{-}$
$\left[\mathrm{NH}_{4}^{+}\right]+\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]+\left[\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}\right]+2\left[\mathrm{HPO}_{4}{ }^{2-}\right]+3\left[\mathrm{PO}_{4}{ }^{3-}\right]$

## Molarity and Formality

These two types of concentration are identical for a species which does not dissociate into ions in solution or does not react with water to produce ions

Molarity is the concentration of the species that is actually present in solution such as $1.0 \mathrm{M} \mathrm{Cl}^{-}$.

Consider a species which forms ions in solution such as acetic acid, $\mathrm{CH}_{3} \mathrm{COOH}$. You might try to place exactly 1.0 mole in a liter of water to form a 1.0 M solution but the solution will have partially dissociated into $\mathrm{CH}_{3} \mathrm{COO}^{-}$. Such a solution is $1.0 \mathrm{~F}=\left[\mathrm{CH}_{3} \mathrm{COOH}\right]+\left[\mathrm{CH}_{3} \mathrm{COO}^{-}\right]$. So formality represents the concentration of the different "pieces" that acetic acid forms in solution or the concentration originally placed in water (before dissociation).

Harris uses formality

## Systematic Treatment of Equilibrium - Mass Balance

EX 3. What is the mass balance equation for a solution prepared by adding 0.100 moles of ammonia to 1.000 L ?
$\mathrm{NH}_{3}$ is a weak base and reacts with water:

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(I)<=>\mathrm{OH}^{-}(a q)+\mathrm{NH}_{4}^{+}(a q)
$$

so the mass balance is

$$
0.100 \mathrm{~F}=\left[\mathrm{NH}_{3}\right]_{\mathrm{o}}=\left[\mathrm{NH}_{3}\right]+\left[\mathrm{NH}_{4}^{+}\right]
$$

## Systematic Treatment of Equilibrium

General approach includes

1. write down the pertinent chemical reactions and their equilibrium constant expressions
2. write down all species present in solution according to \#1
3. set up the charge balance equation (the solution must be electrically neutral so the number of positive charges $=$ the number of negative charges)
4. apply the material balance equation (conservation of matter) - may be more than one
5. are there enough equations to solve for the unknowns?

## Systematic Treatment - Dilute Strong Acid

EX 4. What is the pH of a $1.0 \times 10^{-8} \mathrm{M}$ solution of HBr ?

1. reactions, $\mathrm{K}\left(\mathrm{HBr} \rightarrow \mathrm{H}^{+}+\mathrm{Br}^{-}\right)$
2. species: $\mathrm{H}^{+}, \mathrm{OH}^{-}, \mathrm{Br}^{-}$

$$
\mathrm{H}_{2} \mathrm{O} \Leftrightarrow=>\mathrm{H}^{+}+\mathrm{OH}^{-} \quad K_{\mathrm{w}}=\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right]
$$

3. charge balance: $\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]+[\mathrm{Br}-]$ substitute for $\left[\mathrm{OH}^{-}\right]$
4. mass balance: $\left[\mathrm{Br}^{-}\right]=1.0 \times 10^{-8}$ substitute for $\left[\mathrm{Br}^{-}\right]$

$$
\begin{aligned}
K_{\mathrm{w}} & =\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right]=\left[\mathrm{H}^{+}\right]\left\{\left[\mathrm{H}^{+}\right]-\left[\mathrm{Br}^{-}\right]\right\}=\left[\mathrm{H}^{+}\right]^{2}-\left[\mathrm{H}^{+}\right][\mathrm{Br}-] \\
& \quad \text { quadratic: }\left[\mathrm{H}^{+}\right]^{2}-\left[\mathrm{H}^{+}\right]\left(1.0 \times 10^{-8}\right)-K_{\mathrm{w}}=0 \\
{\left[\mathrm{H}^{+}\right] } & =\left\{-10^{-8} \pm \sqrt{ }\left[\left(10^{-8}\right)^{2}+4\left(1.01 \times 10^{-14}\right)\right]\right\} / 2 \\
& =1.05 \times 10^{-8} \mathrm{M} \\
& =>\mathrm{pH}=6.978=>6.98
\end{aligned}
$$

## Systematic Treatment - Dilute Strong Acid/Base

For dilute strong acids or bases a systematic treatment is only required when the concentration is between $\sim 10^{-8}$ and $10^{-6} \mathrm{M}$. Above $10^{-8}$ one cannot practically make such a dilute solution and below $10^{-6} \mathrm{H}^{+}$from $K_{w}$ is too small a contribution.


## Systematic Treatment - Weak Acid/Base

The acidity of an aqueous solution of $\mathrm{CH}_{3} \mathrm{COOH}$ is determined by its reaction with water:

$$
\mathrm{CH}_{3} \mathrm{COOH}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(I) \Leftrightarrow \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{COO}^{-}(\mathrm{aq})
$$

and quantitatively measured by its acid dissociation constant, $K_{a}$

$$
K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CH}_{3} \mathrm{COO}^{-}\right]}{\left[\mathrm{CH}_{3} \mathrm{COOH}\right]}
$$

where all concentrations are obtained at equilibrium.

## Systematic Treatment - Weak Acid/Base

1. reactions
$\mathrm{H}_{2} \mathrm{O}<=>\mathrm{H}^{+}+\mathrm{OH}^{-} \quad \mathrm{K}_{\mathrm{w}}=\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right]$
2. species: $\mathrm{CH}_{3} \mathrm{COOH}, \mathrm{CH}_{3} \mathrm{COO}^{-}, \mathrm{H}^{+}, \mathrm{OH}^{-}$
3. cb: $\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]+\left[\mathrm{CH}_{3} \mathrm{COO}^{-}\right]$
4. $\mathrm{mb}: 0.01 \mathrm{~F}=\left[\mathrm{CH}_{3} \mathrm{COOH}\right]+\left[\mathrm{CH}_{3} \mathrm{COO}^{-}\right]$
$\mathrm{CH}_{3} \mathrm{COOH}+\mathrm{H}_{2} \mathrm{O}<=>\mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{CH}_{3} \mathrm{COO}^{-}$

$$
K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CH}_{3} \mathrm{COO}^{-}\right]}{\left[\mathrm{CH}_{3} \mathrm{COOH}\right]}=\frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{CH}_{3} \mathrm{COO}^{-}\right]}{0.01-\left[\mathrm{CH}_{3} \mathrm{COO}^{-}\right]}
$$

$$
=\frac{\left[\mathrm{H}^{+}\right]\left\{\left[\mathrm{H}^{+}\right]-\left[\mathrm{OH}^{-}\right]\right\}}{0.01-\left\{\left[\mathrm{H}^{+}\right]-\left[\mathrm{OH}^{-}\right]\right\}}
$$

$$
\mathrm{CH}_{3} \mathrm{COOH} \text { is an acid so }
$$

$$
\left[\mathrm{OH}^{-}\right] \ll\left[\mathrm{H}^{+}\right]
$$

$$
=\frac{\left[\mathrm{H}^{+}\right]\left\{\left[\mathrm{H}^{+}\right]-K_{\mathrm{w}} /\left[\mathrm{H}^{+}\right]\right\}}{0.01-\left\{\left[\mathrm{H}^{+}\right]-K_{\mathrm{w}} /\left[\mathrm{H}^{+}\right]\right\}}
$$

$$
=\frac{\left[\mathrm{H}^{+}\right]^{2}}{0.01-\left[\mathrm{H}^{+}\right]}=\mathrm{K}=\frac{x^{2}}{\mathrm{~F}-x}
$$

## Weak Acid - $K_{\mathrm{a}}=x^{2} I(F-x)$

EX 6. What is the pH of 0.050 M solution of a weak acid, $K_{\mathrm{a}}=1.59 \times 10^{-10}$ ?

$$
\begin{aligned}
& \mathrm{HA}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{I})<=>\mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{A}^{-}(\mathrm{aq}) \\
& 0.050 \mathrm{M} \sim 0 \quad 0 \\
& -x+x+x \\
& 0.050-x \quad x \quad x \\
& K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}=\frac{x^{2}}{0.050-x} \\
& \text { quadratic: } x^{2}+K_{\mathrm{a}} x-0.050 K_{\mathrm{a}}=0 \\
& x=\left\{-1.59 \times 10^{-10} \pm \sqrt{ }\left[\left(1.59 \times 10^{-10}\right)^{2}+4(0.050)\left(1.59 \times 10^{-10}\right)\right]\right\} / 2 \\
& =2.819 \times 10^{-6} \mathrm{M} \quad\left(2.819 \times 10^{-6}\right) / 0.050 \\
& <1 \% \quad 1 \% \text { (5\%) Rule } \\
& =>\mathrm{pH}=5.5498 \Rightarrow 5.55 \quad \mathrm{x}=\sqrt{ }\left(0.050 K_{\mathrm{a}}\right)
\end{aligned}
$$

## Weak Acid Dissociation - $K_{\mathrm{a}}=x^{2} I(\mathrm{~F}-x)$

EX 7. What is the pH of 0.010 and 0.0010 M acetic acid, $K_{\mathrm{a}}=1.76 \times 10^{-5}$, and its fraction of dissociation


$$
K_{\mathrm{a}}=\frac{x^{2}}{\mathrm{M}-x} \quad \text { quadratic: } x^{2}+K_{\mathrm{a}} x-\mathrm{M} K_{\mathrm{a}}=0
$$

a) 0.010 M
$\left[\mathrm{H}^{+}\right]=4.108 \times 10^{-4} \mathrm{M}$
$\mathrm{pH}=3.396$
b) 0.0010
$1.241 \times 10^{-4} \mathrm{M}$
3.906
$\alpha=0.04$
0.1241
fraction dissociation (acids)

$$
\alpha=\left[\mathrm{A}^{-}\right] /[\mathrm{HA}]_{0}
$$

fraction of association (bases)
$\alpha=\left[\mathrm{BH}^{+}\right] /[\mathrm{B}:]_{\text {。 }}$

## Weak Acid Dissociation - $K_{\mathrm{a}}=x^{2} I(F-x)$

$$
\mathrm{CH}_{3} \mathrm{COOH}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(l)<=>\mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{COO}^{-}(\mathrm{aq})
$$

a) 0.010 M
$\left[\mathrm{H}^{+}\right]=4.108 \times 10^{-4} \mathrm{M}$ $\mathrm{pH}=3.396$
$\alpha=0.04$
fraction dissociation (acids)

$$
\alpha=[A-] /[\mathrm{HA}]_{0}
$$

fraction of association (bases)

$$
\alpha=\left[\mathrm{BH}^{+}\right] /[\mathrm{B}:]_{0}
$$

b) 0.0010 M
$1.241 \times 10^{-4} \mathrm{M}$
3.906
0.1241
dilution effect on

1. equilibrium
2. $\left[\mathrm{H}^{+}\right]$
3. pH
4. ionization
$\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\mathrm{n}_{\mathrm{H} 3 \mathrm{O}+} / \mathrm{L}$ of solution

Acid concentration


More dilute

## Weak Base Dissociation - $K_{b}=x^{2} I(F-x)$

EX 8. What is the pH of 0.25 M solution of ammonia, $K_{\mathrm{b}}=1.8 \times 10^{-5}$

$$
\begin{aligned}
& \begin{array}{lcc}
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(I) & <=> & \mathrm{OH}^{-}(a q) \\
M & \sim 0 & \mathrm{NH}_{4}^{+}(a q) \\
-x & +x & 0 \\
M-x & x & x
\end{array} \\
& K_{\mathrm{b}}=\frac{x^{2}}{\mathrm{M}-x} \quad \text { quadratic: } \mathrm{x}^{2}+K_{\mathrm{b}} x-\mathrm{M} K_{\mathrm{b}}=0 \\
& {\left[\mathrm{OH}^{-}\right]=0.00211 \quad \Rightarrow \quad\left[\mathrm{H}^{+}\right]=K_{\mathrm{w}} /\left[\mathrm{OH}^{-}\right]=4.7811 \times 10^{-12} \mathrm{M}} \\
& \text { pH }=11.32
\end{aligned}
$$

## Acid/Base Properties of Salt Solutions

| cation* | anion** | example | pH of solution |
| :---: | :---: | :---: | :---: |
| from strong base | from strong acid (conjugate base of) | $\mathrm{MgI}_{2}, \mathrm{KClO}_{4}$ | neutral |
| from strong base | from weak acid (conjugate base of) | KF, AgCN | basic |
| from weak base (conjugate acid of) | from strong acid (conjugate base of) | $\mathrm{NH}_{4} \mathrm{Br}$ | acidic |
| from weak base (conjugate acid of) | from weak acid (conjugate base of) | $\mathrm{NH}_{4} \mathrm{NO}_{2}$ | acidic if $K_{\mathrm{a}}>K_{\mathrm{b}}$ <br> basic if $K_{\mathrm{b}}>K_{\mathrm{a}}$ <br> neutral if $K_{\mathrm{a}}=K_{\mathrm{b}}$ |
| highly charged metal ion (hydrated in water) | from strong acid (conjugate base of) | $\begin{aligned} & \mathrm{Al}\left(\mathrm{NO}_{3}\right)_{3} \\ & \mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+} \end{aligned}$ | acidic |
| ${ }^{*}$ cation from strong base (Group I and II hydroxides, excluding Be) and silver: <br> $\mathrm{Li}^{+}, \mathrm{Na}^{+}, \mathrm{K}^{+}, \mathrm{Rb}^{+}, \mathrm{Cs}^{+} \quad \mathrm{Mg}^{2+}, \mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}, \mathrm{Ba}^{2+} \quad \mathrm{Ag}^{+}$ |  |  |  |
| $\mathrm{Cl}-, \mathrm{Br}-, \mathrm{I}-\mathrm{ClO}_{4}^{-}, \mathrm{ClO}_{3}^{-}, \mathrm{NO}_{3}^{-}\left(\right.$not $\left.\mathrm{HSO}_{4}^{-}\right)$WHY? $\mathrm{HSO}_{4}^{-}$is the conjugate base of a strong acid => ineffective base but it does have an acidic proton => solutions are acidic |  |  |  |

## Acidity of Aqueous Solutions of Metal Ions

$$
\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}(a q)+\mathrm{H}_{2} \mathrm{O}(a q) \rightleftharpoons \mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{5}(\mathrm{OH})^{2+}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q)
$$



